

THE HONG KONG POLYTECHNIC UNIVERSITY
HONG KONG COMMUNITY COLLEGE

Subject Title : Engineering Economics

Subject Code : CCN3134

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Numerical Answers

Question B1

(a)(ii) The opportunity cost for Annie to accept the offer as a draftsman is \$25,000.

(c)(i) Total fixed cost, $CF = \$7,600$

Total variable cost = \$10,550

Variable cost per unit, $C_v = \$211$

Total cost $CT = 7,600 + 211D$

(c)(ii) $C_{2012}(50 \text{ shops/month} \times 12) = \$18,150/\text{month} \times 12 = \$217,800$

$C_{2017} = \$217,800 (1.1)^5 = \$350,769.078$

Question B2

(b)(ii) For the \$20,000 annuity:
 $PV_0 = \$20,000(P/A, 12\%, 20) = \$149,388.8$

For the increasing uniform gradient, $G = \$1,000$:
 $PV_0 = PV_{(0)}(P/F, 12\%, 1) = \$1,000(P/G, 12\%, 19)(P/F, 12\%, 1) = \$38,392.8249$

The present-equivalent value (PV) at time zero is:
 $= \$149,388.8 + \$38,392.8249 \approx \$18,7781.62$

(c) Effective interest rate = $e^{8\%} - 1 = 8.33\%$

Future value = $\$20,000(F/P, 8.33\%, 10) = \$20,000(1.0833)^{10} \approx \$44,516.13$

Question B3

(a) $PW(\text{Project A}, 15\%)$
 $= -\$10,000 + \$6,000(P/F, 15\%, 1) + \$4,000(P/F, 15\%, 2) + \$2,000(P/F, 15\%, 3)$
 $+ \$1,000(P/F, 15\%, 4) = \128.8

$$\begin{aligned} & \text{PW}(\text{Project A, 20\%}) \\ & = -\$10,000 + \$6,000(\text{P/F}, 20\%, 1) + \$4,000(\text{P/F}, 20\%, 2) + \$2,000(\text{P/F}, 20\%, 3) \\ & \quad + \$1,000(\text{P/F}, 20\%, 4) = -\$582.9 \end{aligned}$$

Thus, $\text{IRR}(\text{Project A}) = 15.90\%$

$$\begin{aligned} & \text{PW}(\text{Project B, 10\%}) \\ & = -\$10,000 + \$1,000(\text{P/F}, 10\%, 1) + \$3,000(\text{P/F}, 10\%, 2) + \$4,000(\text{P/F}, 10\%, 3) \\ & \quad + \$7,000(\text{P/F}, 10\%, 4) = \$1,174.5 \end{aligned}$$

$$\begin{aligned} & \text{PW}(\text{Project B, 15\%}) \\ & = -\$10,000 + \$1,000(\text{P/F}, 15\%, 1) + \$3,000(\text{P/F}, 15\%, 2) + \$4,000(\text{P/F}, 15\%, 3) \\ & \quad + \$7,000(\text{P/F}, 15\%, 4) = -\$229.5 \end{aligned}$$

Thus, $\text{IRR}(\text{Project B}) = 14.18\%$

(b) $\text{PW}(\text{Project A, cost}) = \$10,000$
 $\text{FW}(\text{Project A, revenue})$
 $= \$6,000(\text{F/P}, 10\%, 3) + \$4,000(\text{F/P}, 10\%, 2) + \$2,000(\text{F/P}, 10\%, 1) + \$1,000 = \$16,026$

Thus, $\text{ERR}(\text{Project A}) = 12.51\%$

$\text{PW}(\text{Project B, cost}) = \$10,000$
 $\text{FW}(\text{Project B, revenue})$
 $= \$1,000(\text{F/P}, 10\%, 3) + \$3,000(\text{F/P}, 10\%, 2) + \$4,000(\text{F/P}, 10\%, 1) + \$7,000 = \$16,361$

Thus, $\text{ERR}(\text{Project B}) = 13.10\%$

Question B4

- (e) Remaining Projects should be ranked from F, C, to E, and F will be the base alternative.

Considering Projects C & F:

$$\begin{aligned} & \text{PW}(\text{C-F, 15\%}) \\ & = -\$30,000 + \$10,000(\text{P/A}, 15\%, 5) = \$3,521.6 \end{aligned}$$

$$\begin{aligned} & \text{PW}(\text{C-F, 20\%}) \\ & = -\$30,000 + \$10,000(\text{P/A}, 20\%, 5) = -\$30,000 + \$10,000(2.99061) = -\$93.9 \end{aligned}$$

$\text{IRR}(\text{C-F}) = 19.87\% > \text{MARR}$

Considering Projects C & E:

$$PW(E-C, 0\%) = -\$10,000 + \$10,000(P/F, 0\%, 5) = \$0$$

→ IRR = 0% < MARR → Choose C!

Question B5

(a)(i) SL method:

$$\begin{aligned} &\text{Depreciation expense per year (also at the end of year 4)} \\ &= (\$50,000 - \$2,000) / 5 = \$9,600 \end{aligned}$$

$$\text{Accumulated depreciation at the end of year 4} = \$38,400$$

$$\text{Book value at the end of year 4} = \$50,000 - \$38,400 = \$11,600$$

(a)(ii) UoP method:

$$\begin{aligned} &\text{Depreciation expense per unit of production} \\ &= (\$50,000 - \$2,000) / 1,600 = \$30 \end{aligned}$$

$$\begin{aligned} &\text{Depreciation expense at the end of year 4} \\ &= (\$50,000 - \$2,000)(300 / 1,600) = \$9,000 \end{aligned}$$

$$\begin{aligned} &\text{Accumulated depreciation at the end of year 4} \\ &= (\$50,000 - \$2,000)(1,400 / 1,600) = \$42,000 \end{aligned}$$

$$\text{Book value at the end of year 4} = \$50,000 - \$42,000 = \$8,000$$

(a)(iii) 200% DB method with SL:

End of Year	BV (at the beginning of year)	200% DB	SL	Depreciation selected
1	50,000	20,000	9,600	20,000
2	30,000	12,000	7,000	12,000
3	18,000	7,200	5,333	7,200
4	10,800	4,320	4,400	4,400
5	6,400	2,560	4,400	4,400

$$\text{Depreciation expense at the end of year 4} = \$4,400$$

$$\text{Accumulated depreciation at the end of year 4} = \$43,600$$

$$\text{Book value at the end of year 4} = \$50,000 - \$43,600 = \$6,400$$

Switch-over from DDB to SL occurs at year 4.

(b) Returns of US dollars = Returns of Japanese Yen

$$\rightarrow (1 + 5\%)(1 + \text{rate of change of US}) = (1 + 1\%)$$

→ Rate of change of US = $1.01/1.05 - 1 = -3.81\%$

Therefore, the US dollar is expected to depreciate by 3.81% in this year.

Or

$(1 + 5\%) = (1 + 1\%)(1 + \text{rate of change of Japanese Yen})$

→ Rate of change of Yen = $1.05/1.01 - 1 = 3.96\%$

Therefore, the Japanese Yen is expected to appreciate by 3.96% in this year.

Question B6

(a)(i) Challenger Economic Life:

When N = 1,

→ EUAC = $[\$100,000(F/P, 10\%, 1) + \$50,000 - \$30,000](A/F, 10\%, 1) = \underline{\$130,000}$

When N = 2,

→ EUAC = $[\$100,000(F/P, 10\%, 2) + \$50,000(F/P, 10\%, 1) + \$60,000 - \$30,000](A/F, 10\%, 2) = \underline{\$98,097}$

When N = 3,

→ EUAC = $[\$100,000(F/P, 10\%, 3) + \$50,000(F/P, 10\%, 2) + \$60,000(F/P, 10\%, 1) + \$72,000 - \$30,000](A/F, 10\%, 3) = \underline{\$91,113}$

When N = 4,

→ EUAC = $[\$100,000(F/P, 10\%, 4) + \$50,000(F/P, 10\%, 3) + \$60,000(F/P, 10\%, 2) + \$72,000(F/P, 10\%, 1) + \$86,400 - \$30,000](A/F, 10\%, 4) = \underline{\$90,760}$

When N = 5,

→ EUAC = $[\$100,000(F/P, 10\%, 5) + \$50,000(F/P, 10\%, 4) + \$60,000(F/P, 10\%, 3) + \$72,000(F/P, 10\%, 2) + \$86,400(F/P, 10\%, 1) + \$103,680 - \$30,000](A/F, 10\%, 5) = \underline{\$93,359}$

Thus, the economic life of the new production line is 4 years, as it attains the lowest EUAC.

(a)(ii) Defender Economic Period:

Year	MV (Market Value)	Loss in MV	Cost of Capital	Operating Cost	Marginal Cost
0	\$50,000	–	–	–	–
1	\$40,000	\$10,000	\$5,000	\$50,000	\$65,000
2	\$30,000	\$10,000	\$4,000	\$68,000	\$82,000
3	\$20,000	\$10,000	\$3,000	\$86,000	\$99,000
4					

The most economical period to keep the defender is 2 years as the marginal cost of defender will be larger than the EUAC of the challenger in part (a)(i).

(b) Benefits = $\$20(P/A, 10\%, \infty)(P/F, 10\%, 1) = \181.82 million

Costs = $\$30 + \$50(P/F, 10\%, 1) + \$30(P/F, 10\%, 2) = \100.25 million

B/C ratio = $1.81 > 1$, this project is beneficial to the economy.